

# Recursive method tracing

## Stack based approach

### Simple Example

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What does `mystery(5)` return?

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3;
    else
        return mystery(b - 1) + 2;
}
```

There are 2 recursive calls in `mystery`. Label the recursive calls 1 & 2.

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

Use a stack to keep track of the method calls and the return values.  
The initial call is `mystery(5)`. Abbreviate the method name as `m`.

`m(5)`

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

$m(5)$  stops at the line labeled **Call 2** when it calls  $m(4)$ .

Use a subscript to note the call  $m(5)$  stopped at.

Add the new call to  $m(4)$  to the top of the stack.

$m(4)$

$m(5)_2$

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

`m(4)` stops at **Call 1** and calls `m(3)`.

`m(3)`

`m(4)`<sub>1</sub>

`m(5)`<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

m(2)

m(3)<sub>2</sub>

m(4)<sub>1</sub>

m(5)<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

m(1)

m(2)<sub>1</sub>

m(3)<sub>2</sub>

m(4)<sub>1</sub>

m(5)<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```



m(0)

m(1)<sub>2</sub>

m(2)<sub>1</sub>

m(3)<sub>2</sub>

m(4)<sub>1</sub>

m(5)<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

`m(0)` returns 0 and terminates.

Cross out the call to `m(0)` to indicate that the method has terminated.

Write the return value to the right of the method.

~~`m(0)`~~ returns 0

`m(1)`<sub>2</sub>

`m(2)`<sub>1</sub>

`m(3)`<sub>2</sub>

`m(4)`<sub>1</sub>

`m(5)`<sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

Control returns to the topmost non-terminated method on the stack,  $m(1)$ .

$m(1)$  was suspended on the line labeled Call 2 when it called  $m(0)$ .

The call to  $m(0)$  returned 0.

$m(1)$  returns  $0 + 2 = 2$ .

~~$m(0)$~~  returns 0

~~$m(1)$~~ <sub>2</sub> returns 2

$m(2)$ <sub>1</sub>

$m(3)$ <sub>2</sub>

$m(4)$ <sub>1</sub>

$m(5)$ <sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

Control returns to  $m(2)$  which was suspended on the line labeled **Call 1**.

The call to  $m(1)$  returned 2.

$m(2)$  returns  $2 + 3 = 5$ .

~~$m(0)$~~  returns 0

~~$m(1)$~~ <sub>2</sub> returns 2

~~$m(2)$~~ <sub>±</sub> returns 5

$m(3)$ <sub>2</sub>

$m(4)$ <sub>1</sub>

$m(5)$ <sub>2</sub>

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

<del>m(0)</del>	returns 0
<del>m(1)</del> <sub>2</sub>	returns 2
<del>m(2)</del> <sub>±</sub>	returns 5
<del>m(3)</del> <sub>2</sub>	returns 7
m(4) <sub>1</sub>	
m(5) <sub>2</sub>	

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

<del>m(0)</del>	returns 0
<del>m(1)</del> <sub>2</sub>	returns 2
<del>m(2)</del> <sub>±</sub>	returns 5
<del>m(3)</del> <sub>2</sub>	returns 7
<del>m(4)</del> <sub>±</sub>	returns 10
m(5) <sub>2</sub>	

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```

<del>m(0)</del>	returns 0
<del>m(1)</del> <sub>2</sub>	returns 2
<del>m(2)</del> <sub>±</sub>	returns 5
<del>m(3)</del> <sub>2</sub>	returns 7
<del>m(4)</del> <sub>±</sub>	returns 10
<del>m(5)</del> <sub>2</sub>	returns 12

```
public int mystery(int b)
{
    if (b == 0)
        return 0;

    if (b % 2 == 0)
        return mystery(b - 1) + 3; // Call 1
    else
        return mystery(b - 1) + 2; // Call 2
}
```